

# Astronomical observation through the earth atmosphere

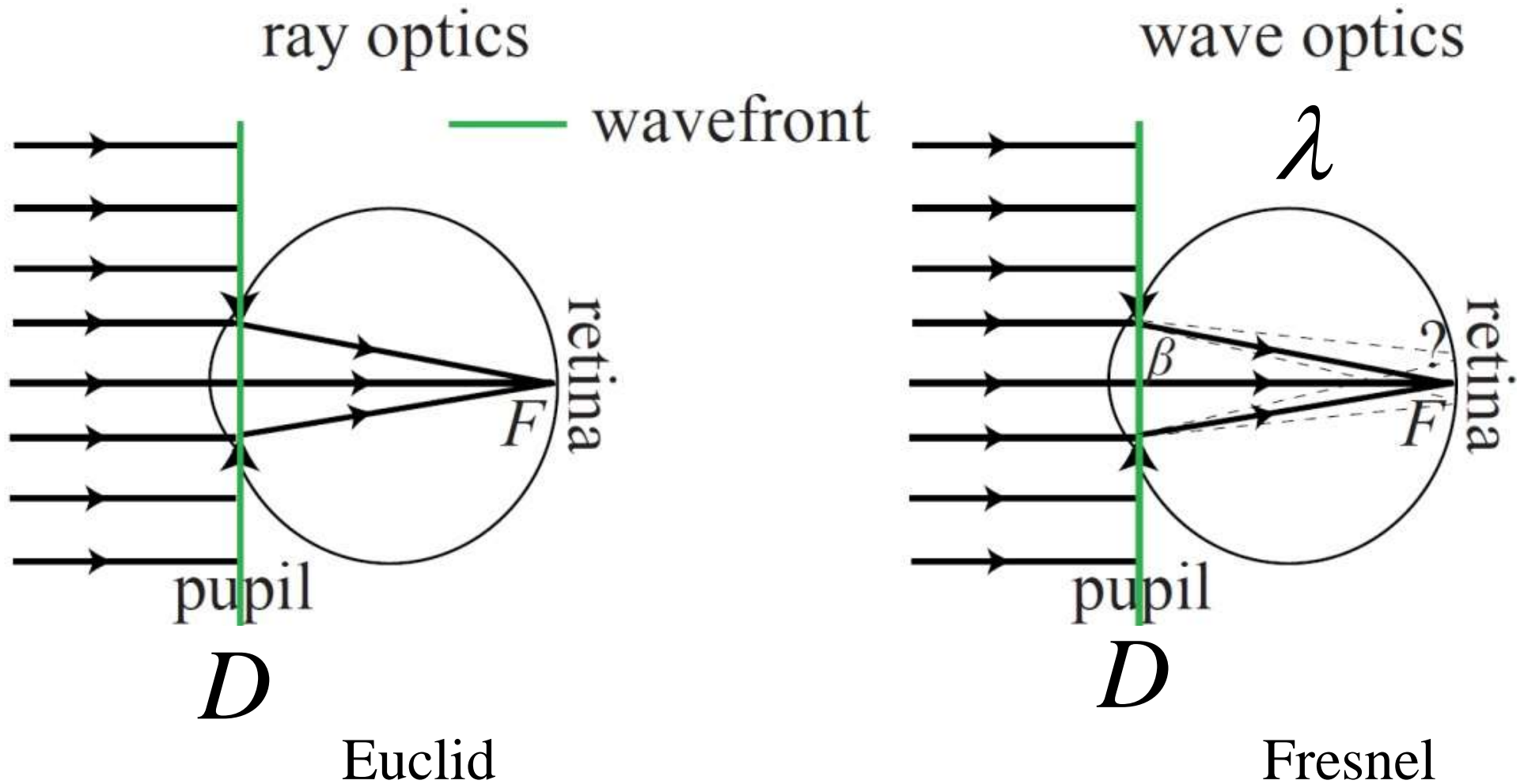
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Technical University Delft

# Astronomical observation through the earth atmosphere

- 1) Limit to angular resolution
- 2) Observation with the aid of a telescope;
  - telescope types
  - image field
  - influence of telescope aberration
- 3) Influence of the earth atmosphere;
  - effect on resolution
  - E-ELT and the 'resolution solution'

# Intensity distribution on the retina

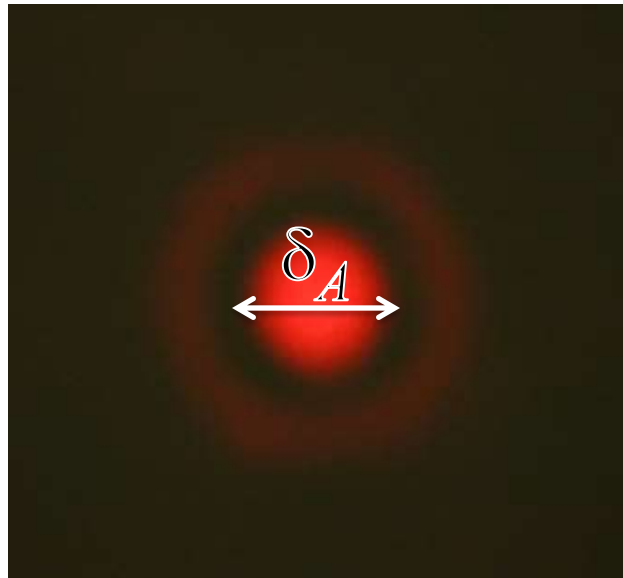


# Intensity distribution in focus

George B. Airy (1801-1892), Astronomer Royal 1835-1881

Publication:

“On the diffraction of an object glass”,  
Transactions of the Philosophical Society of Cambridge,  
Vol. 5, page 283 - 291 (1835).



$$\delta_A = \left( 2.4 \frac{\lambda}{D} \right) f$$
$$= 2 \alpha_A f$$

Eye:

$$\alpha_A = 0.0002$$
$$\approx 1'$$

$n$	$\phi(n)$
0,0	+ 1,0000
0,2	+ ,9950
0,4	+ ,9801
0,6	+ ,9557
0,8	+ ,9221
1,0	+ ,8801
1,2	+ ,8305
1,4	+ ,7742
1,6	+ ,7124
1,8	+ ,6461
2,0	+ ,5767
2,2	+ ,5054
2,4	+ ,4335
2,6	+ ,3622
2,8	+ ,2927
3,0	+ ,2261
3,2	+ ,1633
3,4	+ ,1054
3,6	+ ,0530
3,8	+ ,0067
4,0	- ,0330
4,2	- ,0660
4,4	- ,0992

# Illustration of two-star resolution



# Testing of two-star resolution

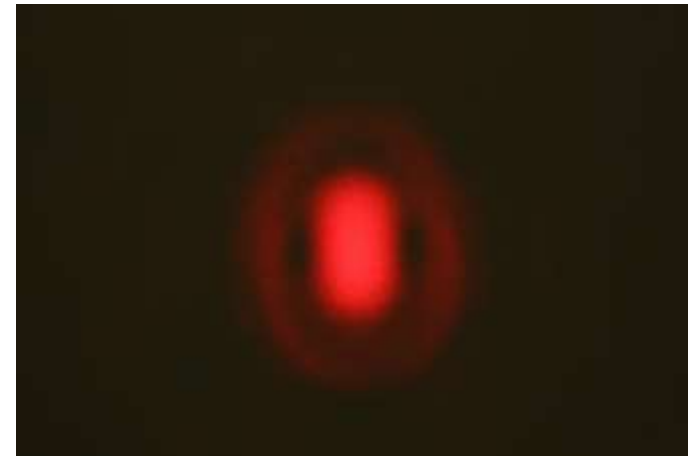
A

$$s = 1.2 \delta_A$$



B

$$s = 0.6 \delta_A$$



Rayleigh  
criterion

C

$$s = 0.3 \delta_A$$



D

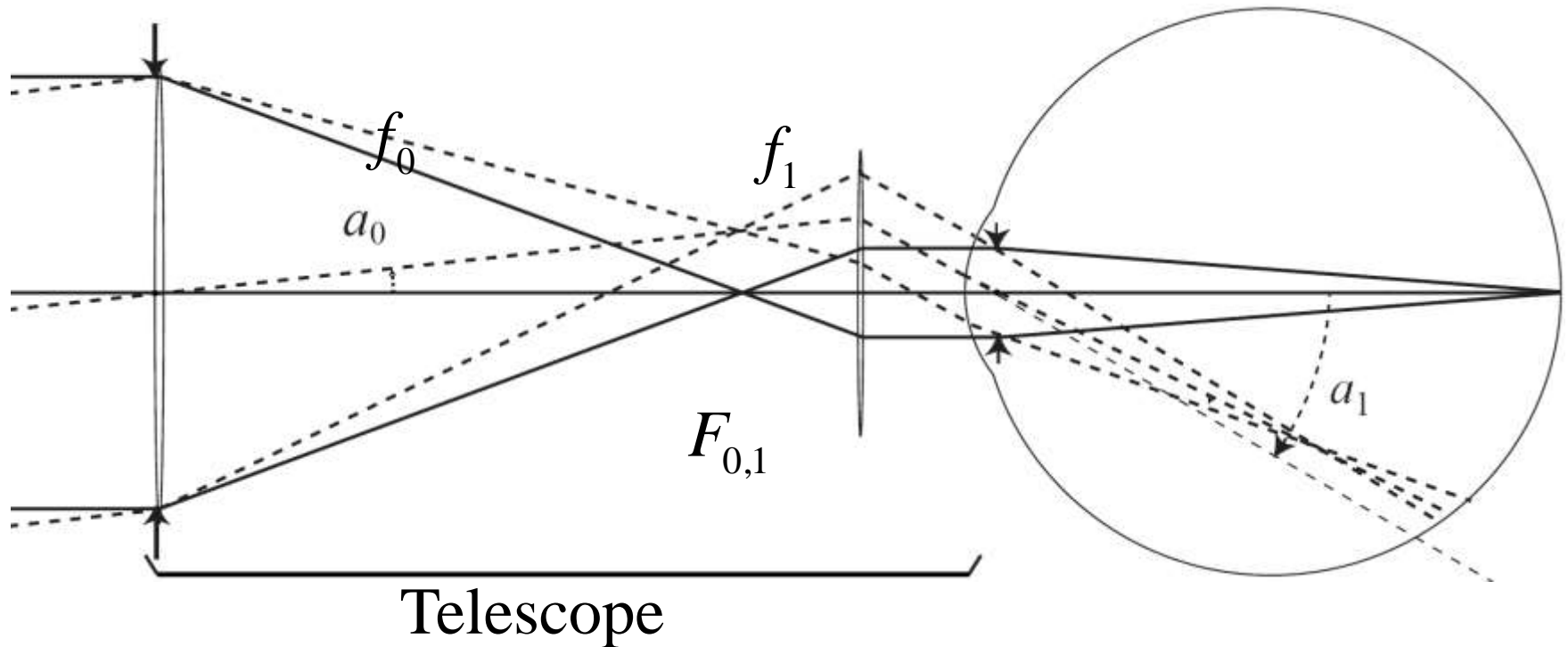
$$s = 0$$



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# Lens telescope and (angular) magnification



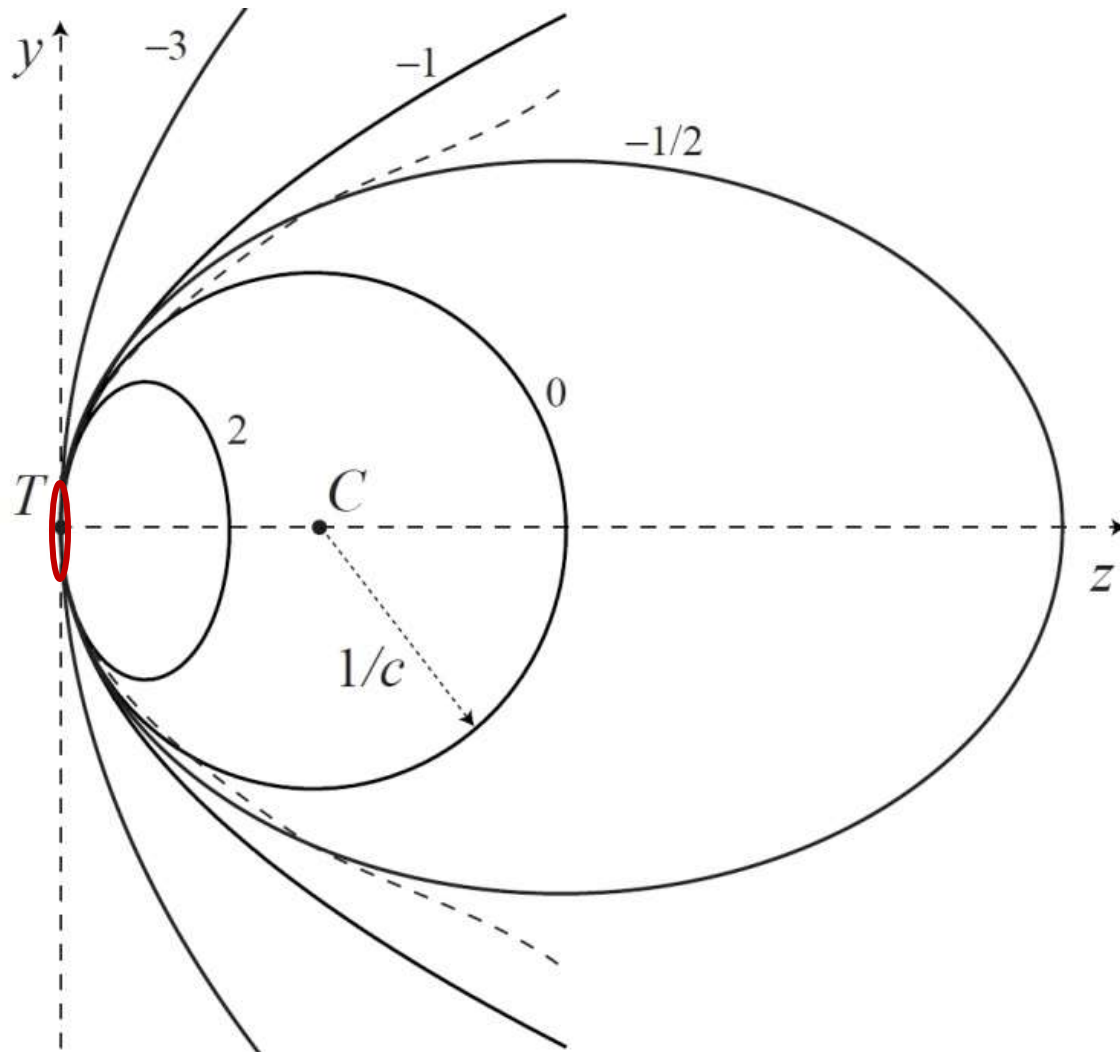
$$\text{Telescope: } m_A = \frac{a_1}{a_0} = \frac{f_0}{f_1} \quad m_T = \frac{a_0}{a_1} = \frac{f_1}{f_0}$$

Irradiance of a star image on the retina is  $m_A^2$  **LARGER**

First observations with lens telescope by G. Galilei



# Mirror telescope and aspheric surfaces (conic sections and general aspheres)



Conic constant  $\kappa$

$\kappa < -1$       hyperbola

$\kappa = -1$       parabola

$-1 < \kappa < 0$       prolate ellipse

$\kappa = 0$       sphere

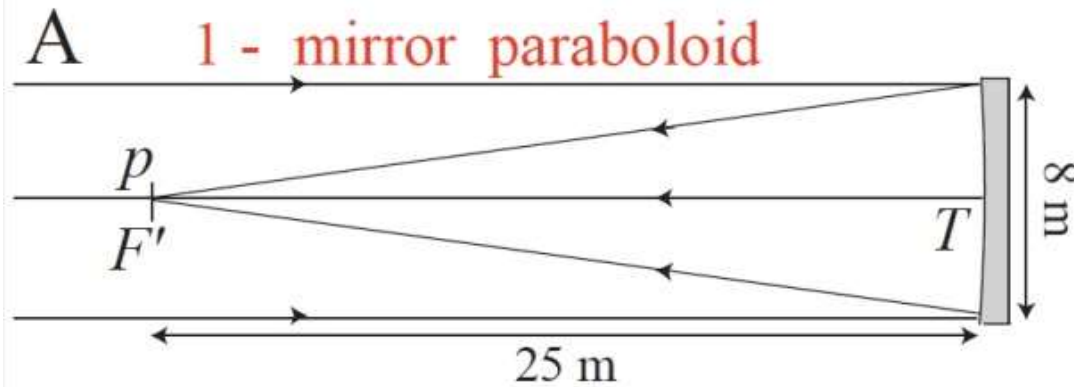
$\kappa > 0$       oblate ellipse

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- - - - General Asphere

# Mirror telescopes (8 m primary)

Theoretical resolution:  
16 milli-arcsec =  $8 \times 10^{-8}$



$$p = 0.7 \text{ mm}$$
$$2a_0 = 3 \cdot 10^{-5} = 6''$$
$$N = 5 \cdot 10^{+4}$$

COMA



$$p = 40 \text{ mm}$$
$$2a_0 = 6 \cdot 10^{-4} = 2'$$
$$N = 10^{+8}$$

COMA



$$p = 100 \text{ mm}$$
$$2a_0 = 15 \cdot 10^{-4} = 5'$$
$$N = 6 \cdot 10^{+8}$$

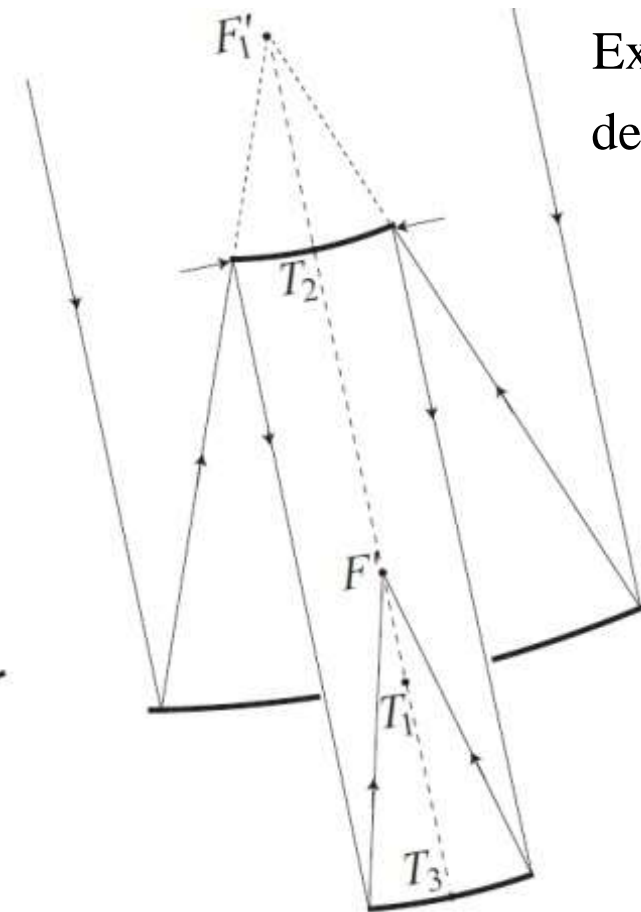
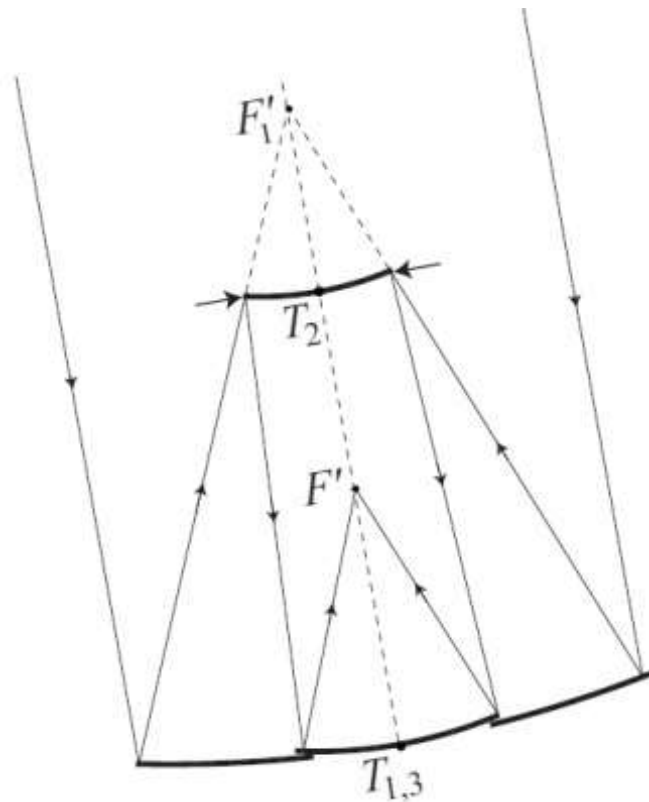
ASTIGMATISM

# Three-mirror telescopes

M. Paul (1935)

Paul - Baker (1969)

Theoretical resolution ELT  
3.4 milli-arcsec =  $1.7 \times 10^{-8}$   
(5 meter on the moon)



Example of a classical Paul-Baker design (primary mirror 39 m diameter)

NO COMA

**NO ASTIGMATISM**

**NO FIELD CURVATURE**

$f' = 75$  m

$p = 500$  mm (sensor size)

$2a_0 = 6.4 \times 10^{-3} = 23' = 0.38^\circ$

$N \approx 10^{+11}$

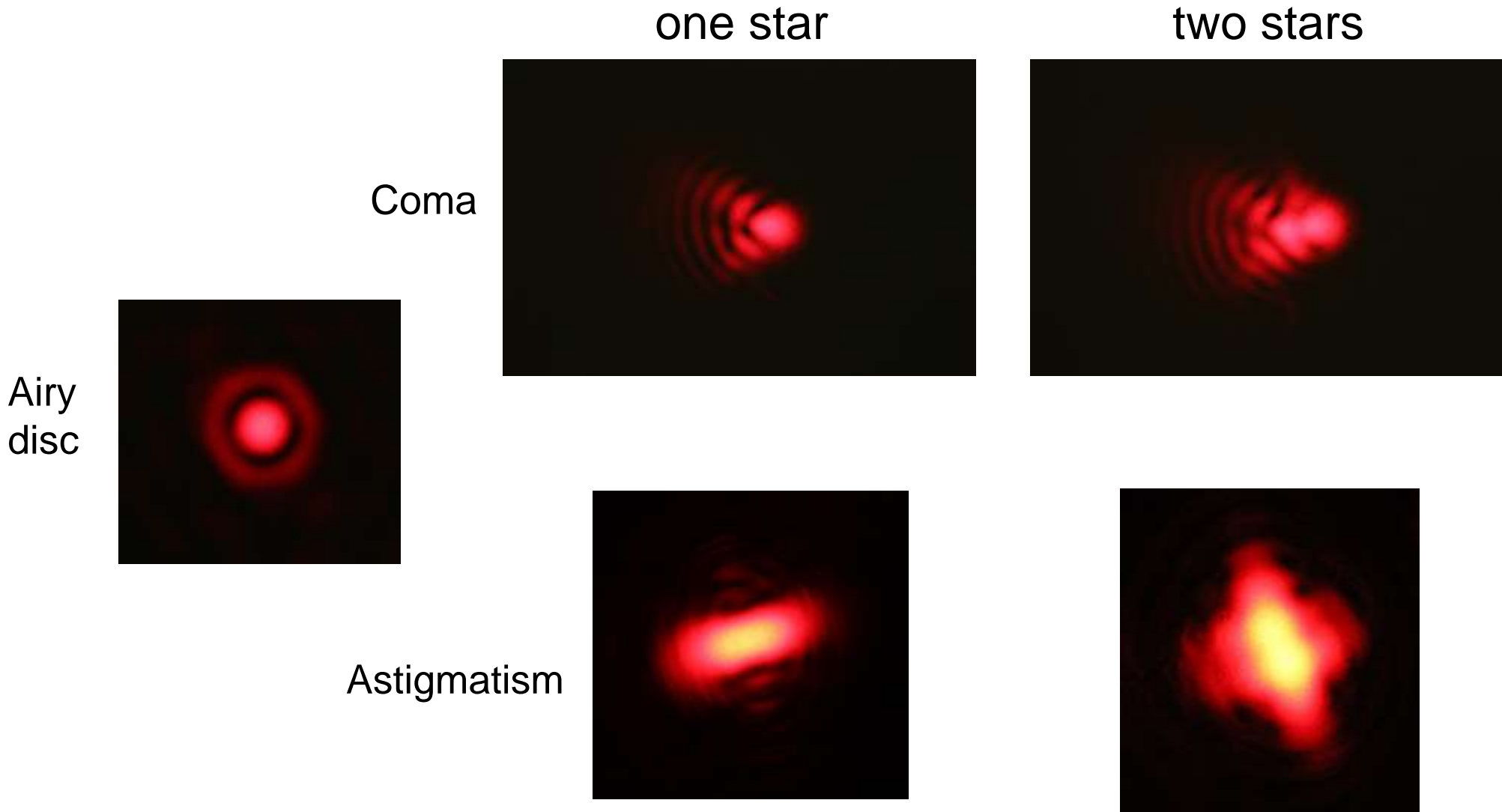
# Three-mirror Paul-Baker telescope

## Classical layout with general aspheres (39 meter primary)

Paul-Baker-anastigmat, $f' = 75$ m, $\lambda = 550$ nm.				
$d_1 = \infty$	$c_1$	-0.0100136102		
	$a_{2,1}$	$-0.50068051 \cdot 10^{-02}$	$a_{4,1}$	$-0.29095457 \cdot 10^{-09}$
	$a_{6,1}$	$-0.63862737 \cdot 10^{-12}$	$a_{8,1}$	$-0.45324414 \cdot 10^{-16}$
$d_2 = -33.3333$	$c_2$	-0.030177320		
	$a_{2,2}$	$-0.15088660 \cdot 10^{-01}$	$a_{4,2}$	$-0.10647662 \cdot 10^{-05}$
	$a_{6,2}$	$-0.20207273 \cdot 10^{-08}$	$a_{8,2}$	$-0.15802737 \cdot 10^{-11}$
	$a_{10,2}$	$-0.23585205 \cdot 10^{-14}$		
$d_3 = +50.0000$	$c_3$	-0.020000000		
	$a_{2,3}$	$-0.10000000 \cdot 10^{-01}$	$a_{4,3}$	$-0.10052010 \cdot 10^{-05}$
	$a_{6,3}$	$-0.20202048 \cdot 10^{-09}$	$a_{8,3}$	$-0.52424597 \cdot 10^{-13}$
$d_4 = -25.06799900$				
Image quality	field angle $\gamma$		$OPD_{rms}$ (units of $\lambda$ )	
	0.0'		0.038	
	3.7'		0.030	
	7.3'		0.014	
	10.3'		0.040	
	11.0'		0.051	

general aspheres

# Telescope aberrations: coma and astigmatism

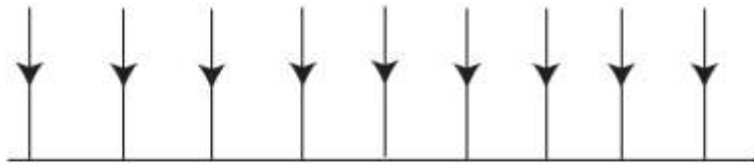


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  - angular resolution
  
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# Atmospheric turbulence ('seeing')

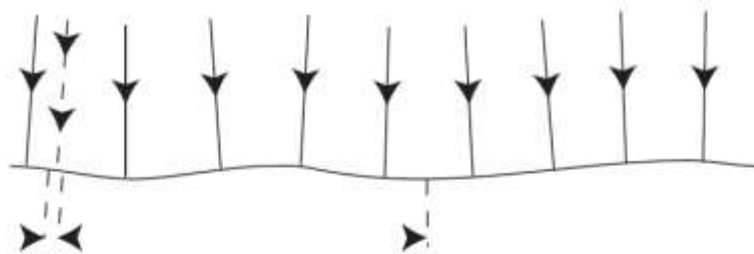
Star light



wavefront

## ATMOSPHERE

angular spread rays: 0.8 to 1.2 arcsec



wavefront deviation: several micrometers

eye pupil

(4 mm)

NO BLUR,  
ONLY TILT

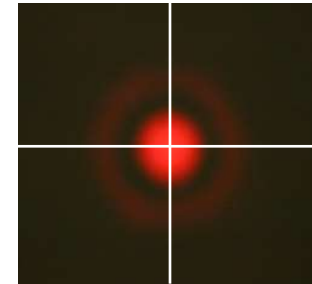
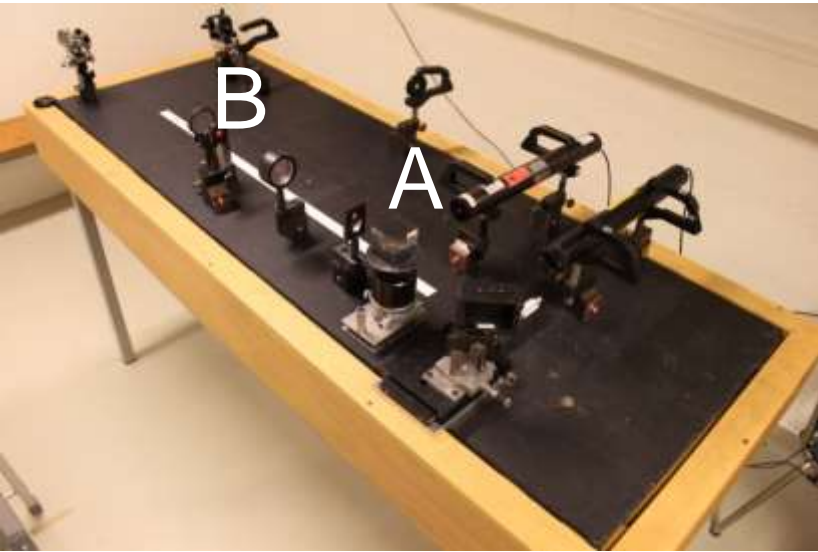
E-ELT primary

(39000 mm)

SEVERE BLURRING  
AND TILT

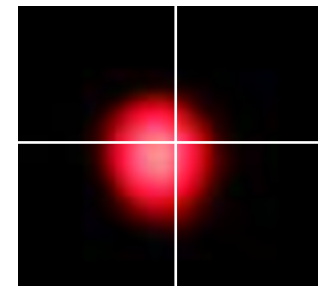


# Atmospheric turbulence ('seeing')



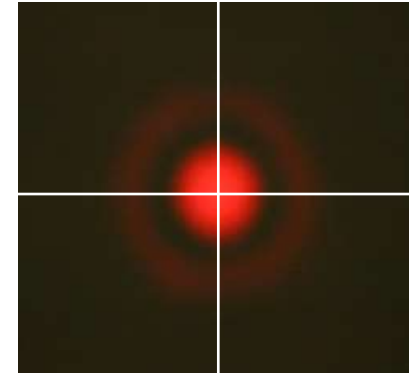
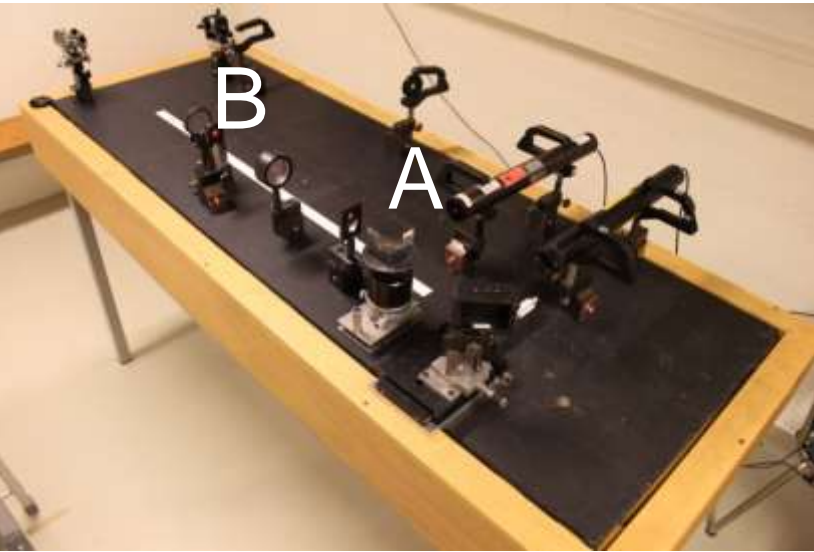
small-sized beam, 'weak turbulence'  
→ time-dependent shift of star image

A

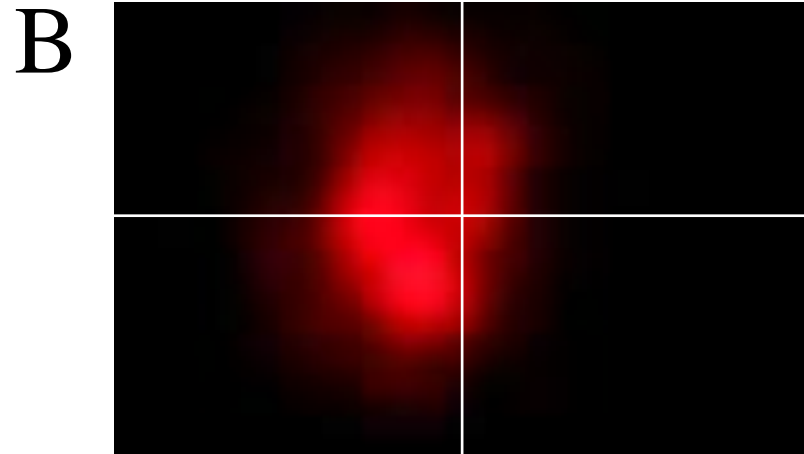




# Atmospheric turbulence ('seeing')



5x larger beam, 'stronger turbulence'  
→ blur AND shift of star image



# Conclusions

- a (passive) 39 meter telescope is unique with respect to light collection
- all mirror surfaces should be individually measured and adjusted down to a fraction (50 nanometer) of the wavelength of visible light ( $\lambda=550$  nanometer)
- `seeing' at E-ELT-site is of the order of **0.8 arcsec** (0.3 arcsec record low value)  
→ enormous gap with the theoretical resolution of E-ELT: **0.0034 arcsec**
- full imaging capability of the 39-meter telescope requires
  - mechanical deformations add up to optical aberrations smaller than **100 nm**
  - seeing effects should be cancelled over an area of **1100 square meters**

**HERCULEAN TASK for the E-ELT team of the  
European Southern Observatory**